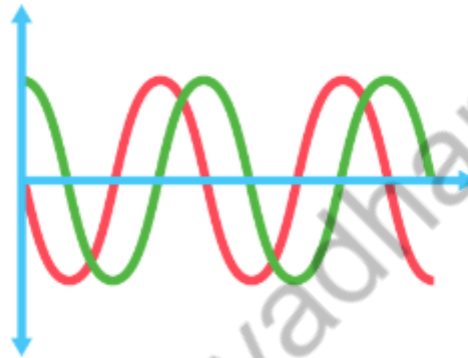


Course: Advanced Analog IC Design



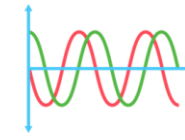
Lecture 2: Switched-Capacitor Circuits

Reference: Design of Analog CMOS Integrated Circuits by Behzad Razavi

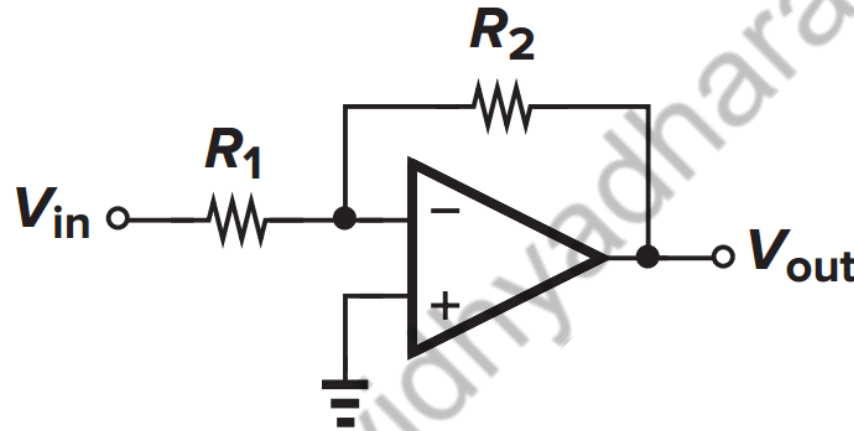
Prof. Sanjay Vidhyadharan



website: sanjayvidhyadharan.in



Simple Continuous Time Amplifier

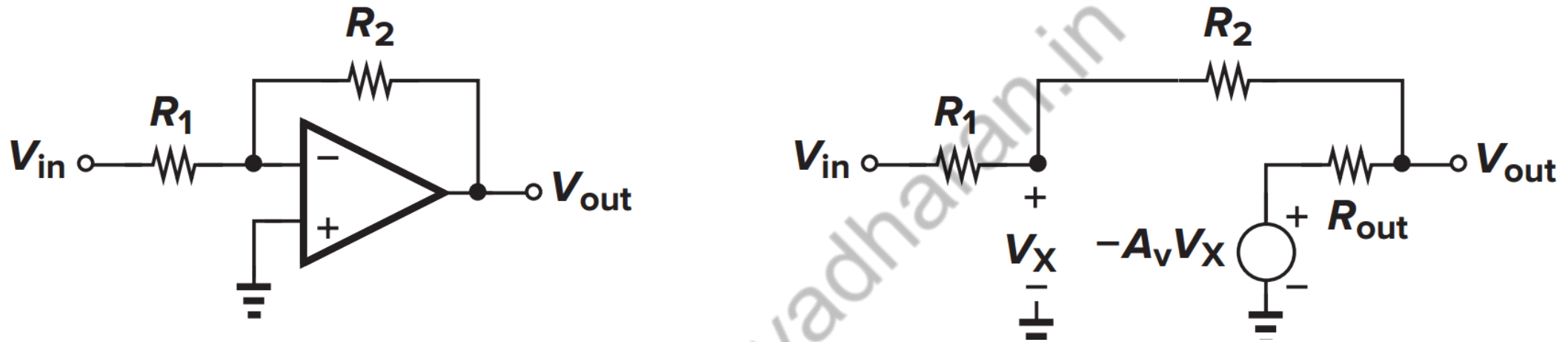


$$V_{in} / R_1 = - V_{out} / R_2$$

$$\text{Gain} = -R_2 / R_1.$$

1. General Considerations

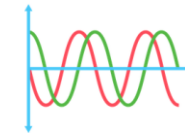
Simple Continuous Time Amplifier



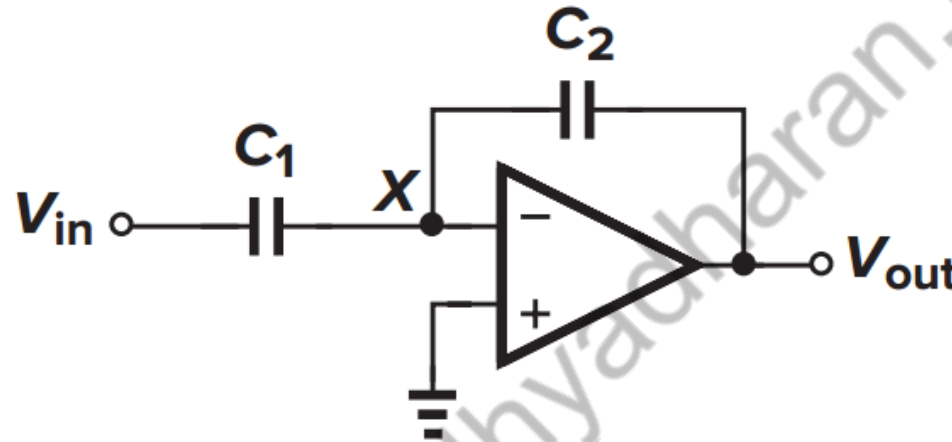
$$-A_v \left(\frac{V_{out} - V_{in}}{R_1 + R_2} R_1 + V_{in} \right) - R_{out} \frac{V_{out} - V_{in}}{R_1 + R_2} = V_{out}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1} \cdot \frac{A_v - \frac{R_{out}}{R_2}}{1 + \frac{R_{out}}{R_1} + A_v + \frac{R_2}{R_1}}$$

1. Closed-loop gain suffers from inaccuracies
2. Input resistance of the amplifier, approximately equal to R_1 , loads the preceding stage. R_1 has to be low for High gain. While high R_1 while introducing thermal noise .
3. $R_{out}/R_2 \ll A_v$



Simple continuous time amplifier with Capacitors

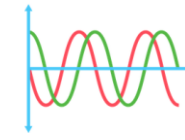


$$V_{in} * C_1 \omega = - V_{out} * C_2 \omega$$

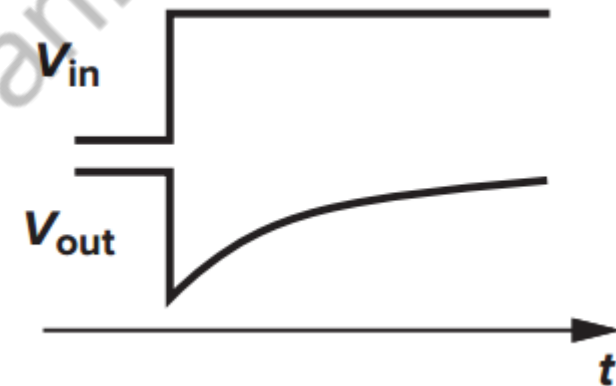
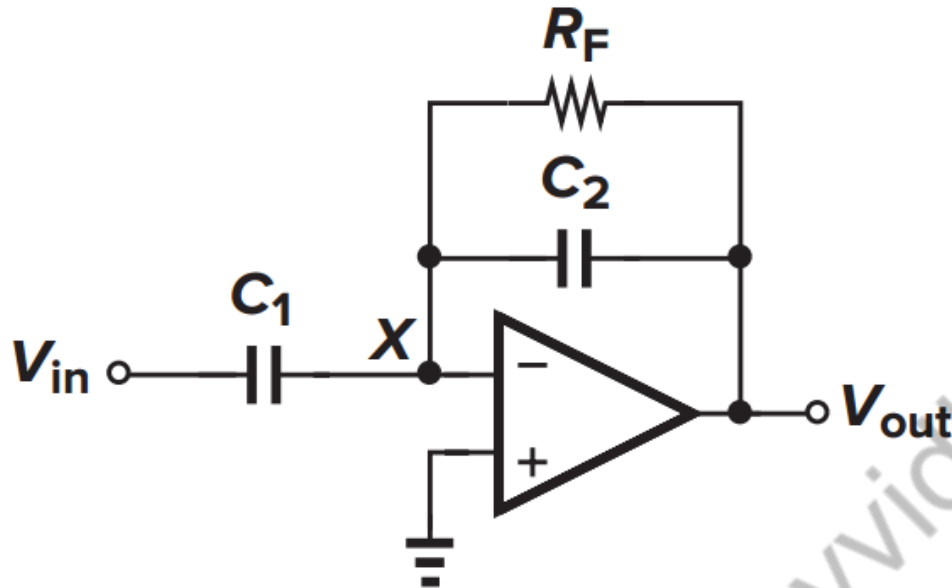
$$\text{Gain} = -C_1/C_2.$$

No Noise . Less Area requirement

1. No DC feedback.
2. Can get Saturated due to offset



Simple continuous time amplifier with Capacitors



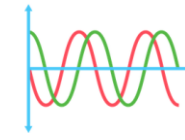
Step response

1. Only useful for High Frequencies
2. Large R_F requires more silicon area
3. Circuit may not be suited to amplify wideband

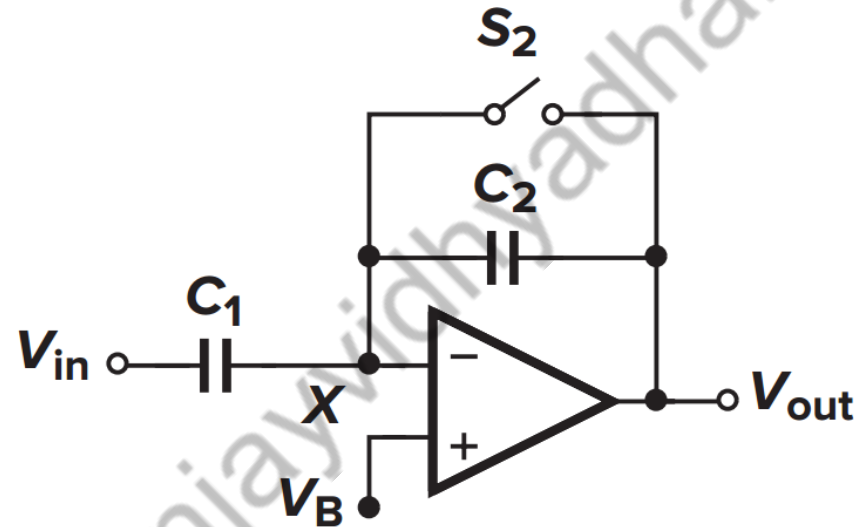
$$\begin{aligned}\frac{V_{out}}{V_{in}}(s) &\approx -\frac{R_F \frac{1}{C_2 s}}{R_F + \frac{1}{C_2 s}} \div \frac{1}{C_1 s} \\ &= -\frac{R_F C_1 s}{R_F C_2 s + 1}\end{aligned}$$

$$V_{out}/V_{in} \approx -C_1/C_2 \text{ only if } \omega \gg (R_F C_2)^{-1}$$

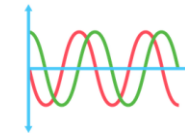
2. Switched Capacitance Amps



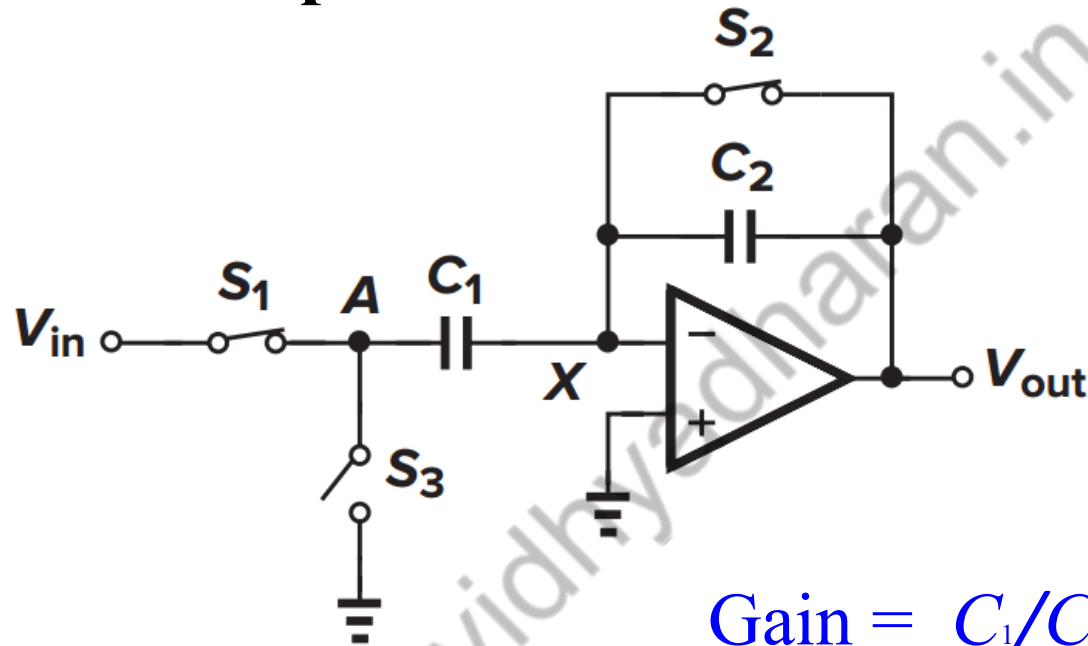
Use of feedback switch to define dc input level



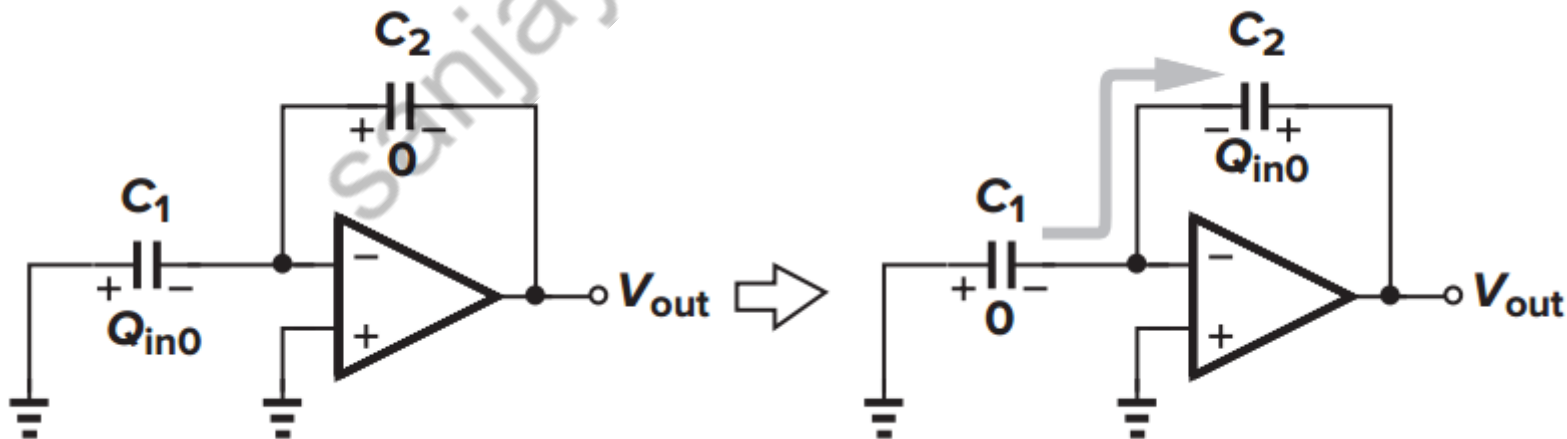
2. Switched Capacitance Amps



Switched-capacitor amplifier.

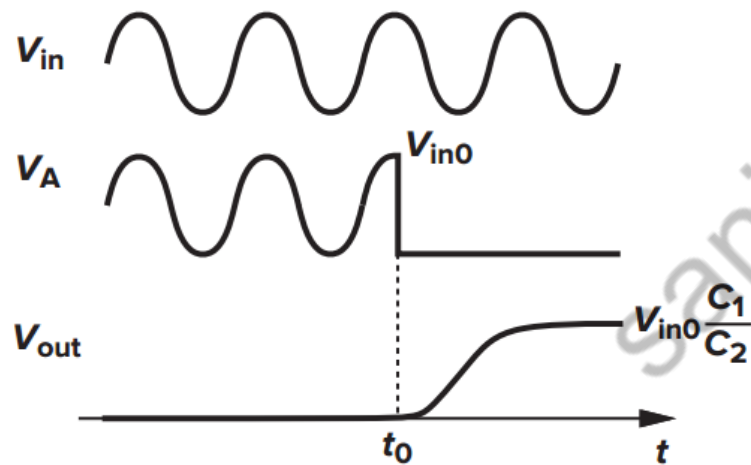
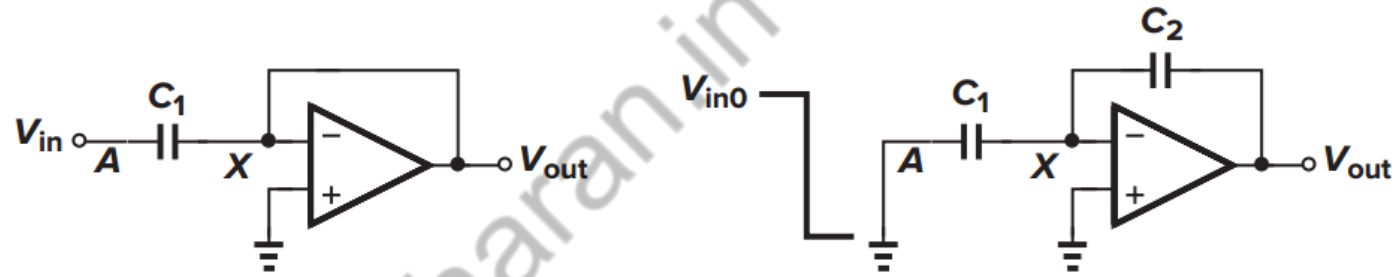
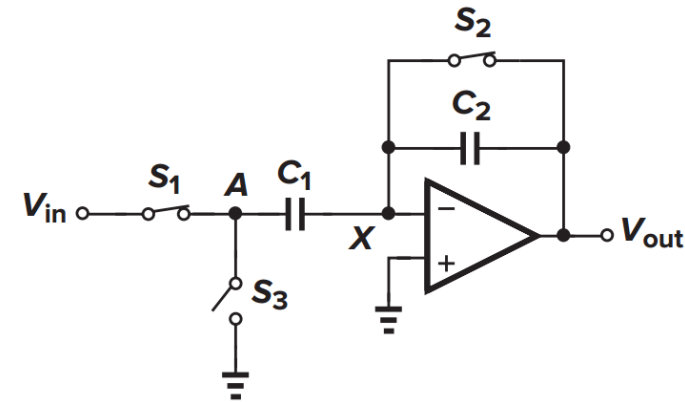


$$\text{Gain} = C_1/C_2.$$



2. Switched Capacitance Amps

Switched-capacitor amplifier.



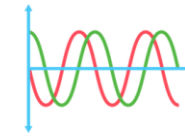
1. During sampling the input, output set to zero

2. After sampling, for $t > t_0$, the circuit ignores the input voltage amplifying the sampled voltage

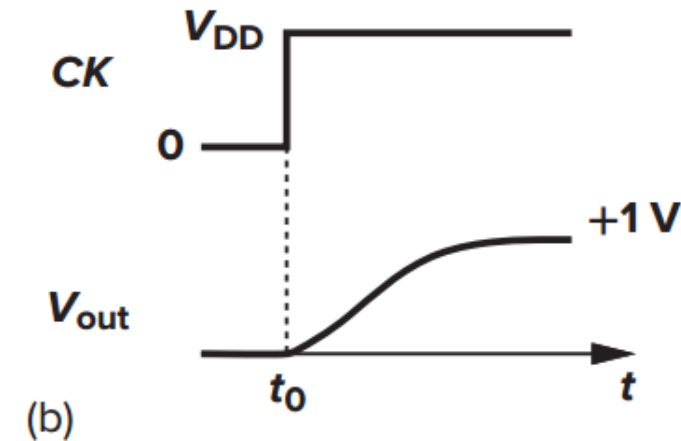
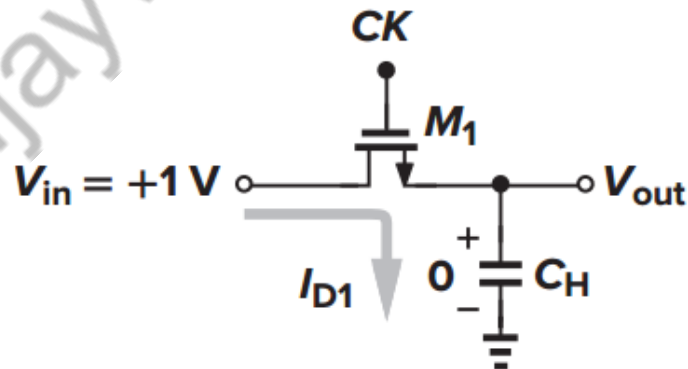
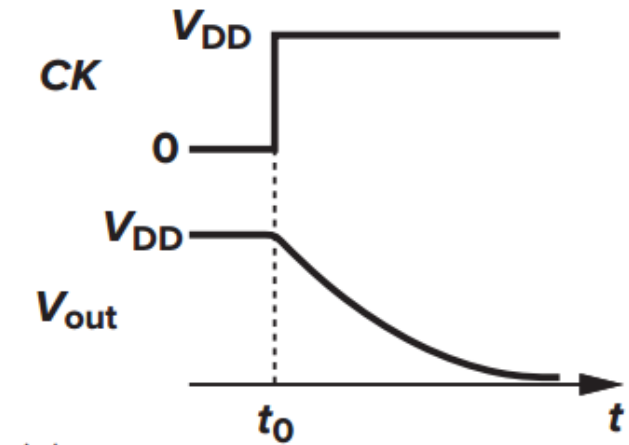
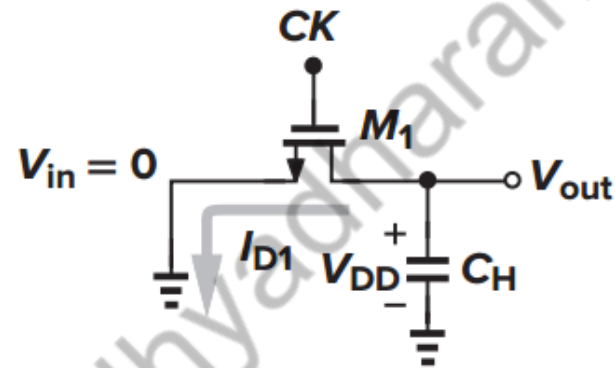
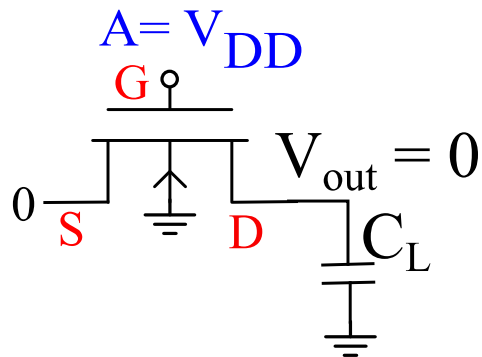
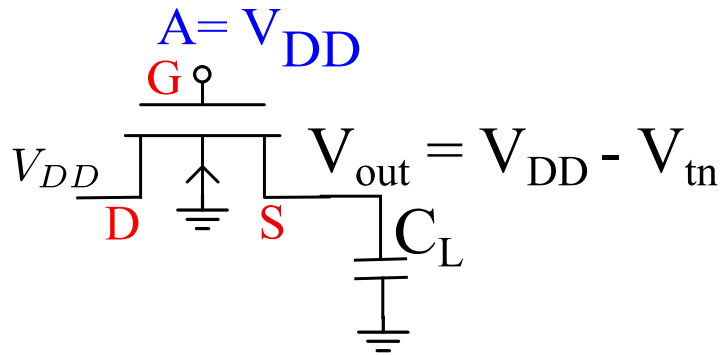
3. Note that S2 must turn on periodically to compensate for the leakage currents

1. V_{out} settles to $V_{in} \cdot C_1 / C_2$, the current through C_2 approaches zero. That is, the feedback capacitor does not reduce the open-loop gain of the amplifier if the output voltage is given enough time to settle. On the other hand, R_2 loads the amplifier continuously.

3. Sampling Switches

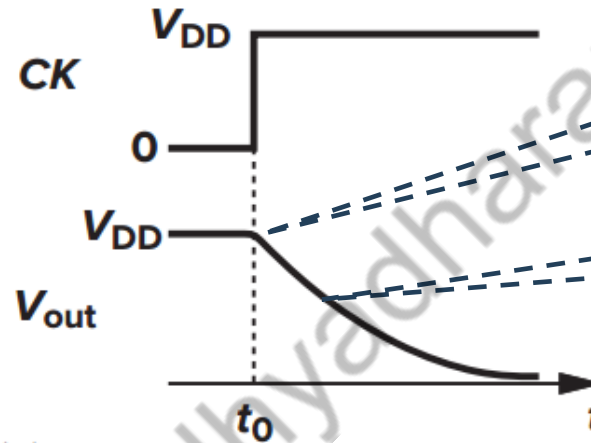
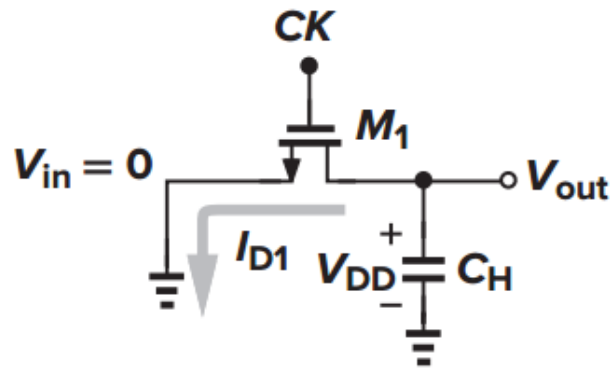


MOSFETS as Switches



3. Sampling Switches

MOSFETS as Switches

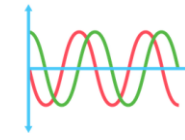


$$I_D = \frac{\mu_n C_{ox} W (V_{DD} - V_T)^2}{2L}$$

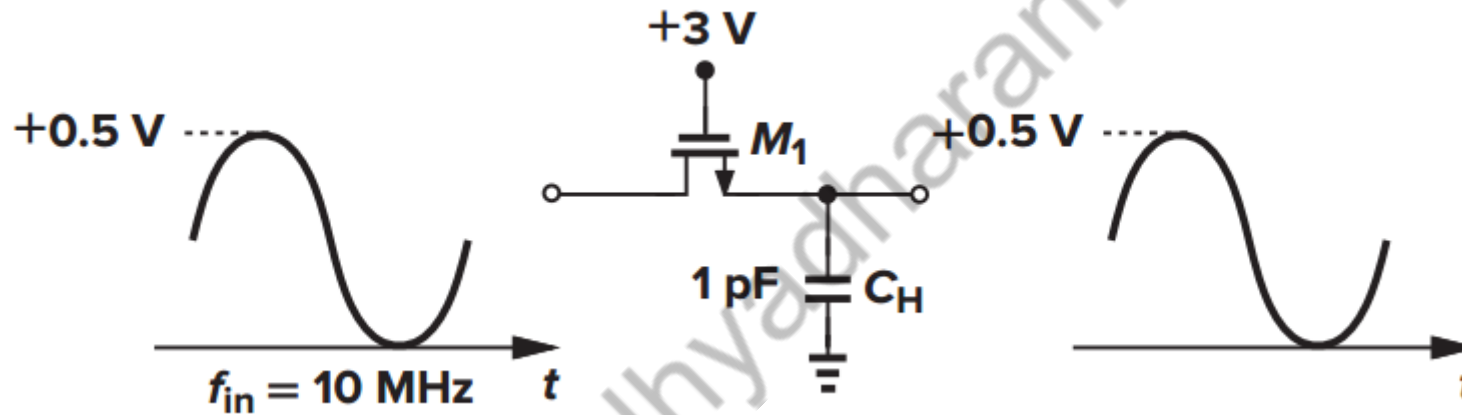
$$V_{out} = V_{DD} - V_{tn}$$

Triode

3. Sampling Switches



MOSFETS as Switches

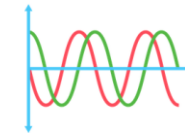


$$I_D = \frac{\mu_n C_{ox} W (V_{GS} - V_T) V_{DS}}{L}$$

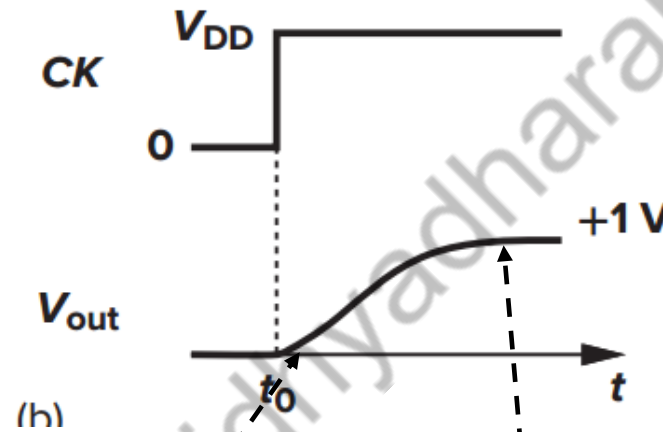
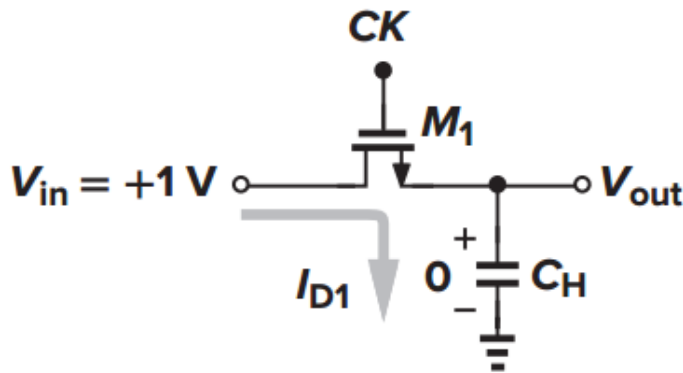
Assuming that $V_{out} \approx V_{in}$,

$$R_{on1} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{in} - V_{TH})}$$

3. Sampling Switches



MOSFETS as Switches

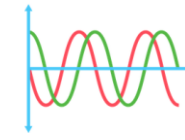


$$I_D = \frac{\mu_n C_{ox} W (V_{GS} - V_T) V_{DS}}{L}$$

$$R_{on} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{TH})}$$

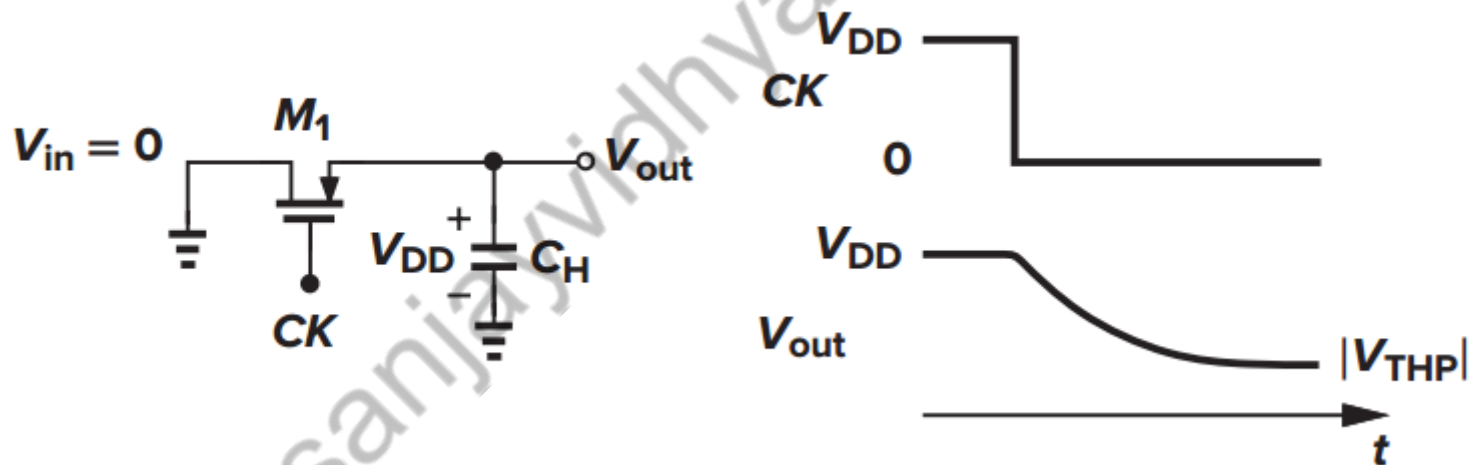
$$I_D = \frac{\mu_n C_{ox} W (V_{GS} - V_T) V_{DS}}{L}$$

3. Sampling Switches



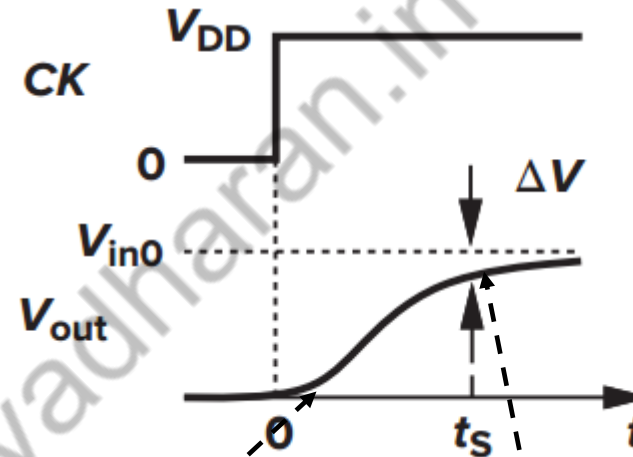
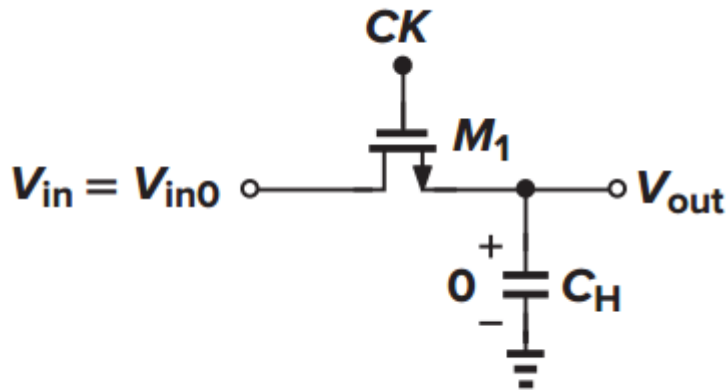
MOSFETS as Switches

Sampling circuit using PMOS switch



3. Sampling Switches

Speed Considerations



Sampling speed is given by two factors:

ON resistance of the switch

Value of the sampling capacitor

$$R_{on} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{TH})}$$

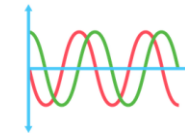
$$R_{on1} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{in} - V_{TH})}$$

Ron also depends on the input level For example, if we restrict the variation of Ron to a range of 4 to 1, then the maximum input level is given by

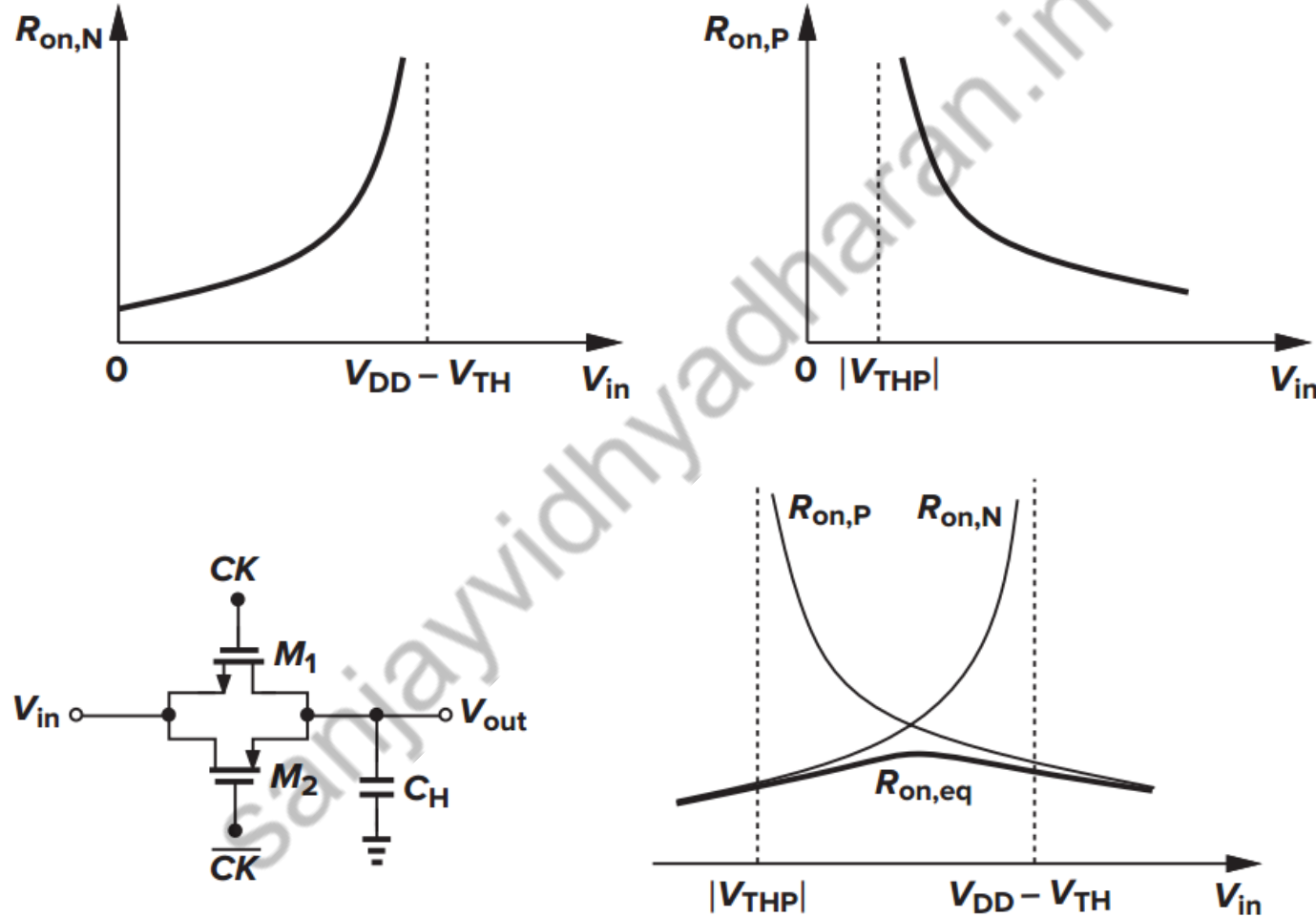
$$\frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{in,max} - V_{TH})} = \frac{4}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{TH})}$$

This value falls around $V_{DD}/2$, translating to severe swing limitations.
Device threshold voltage directly limits the voltage swings.

3. Sampling Switches

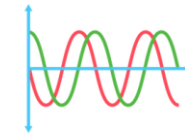


Speed Considerations



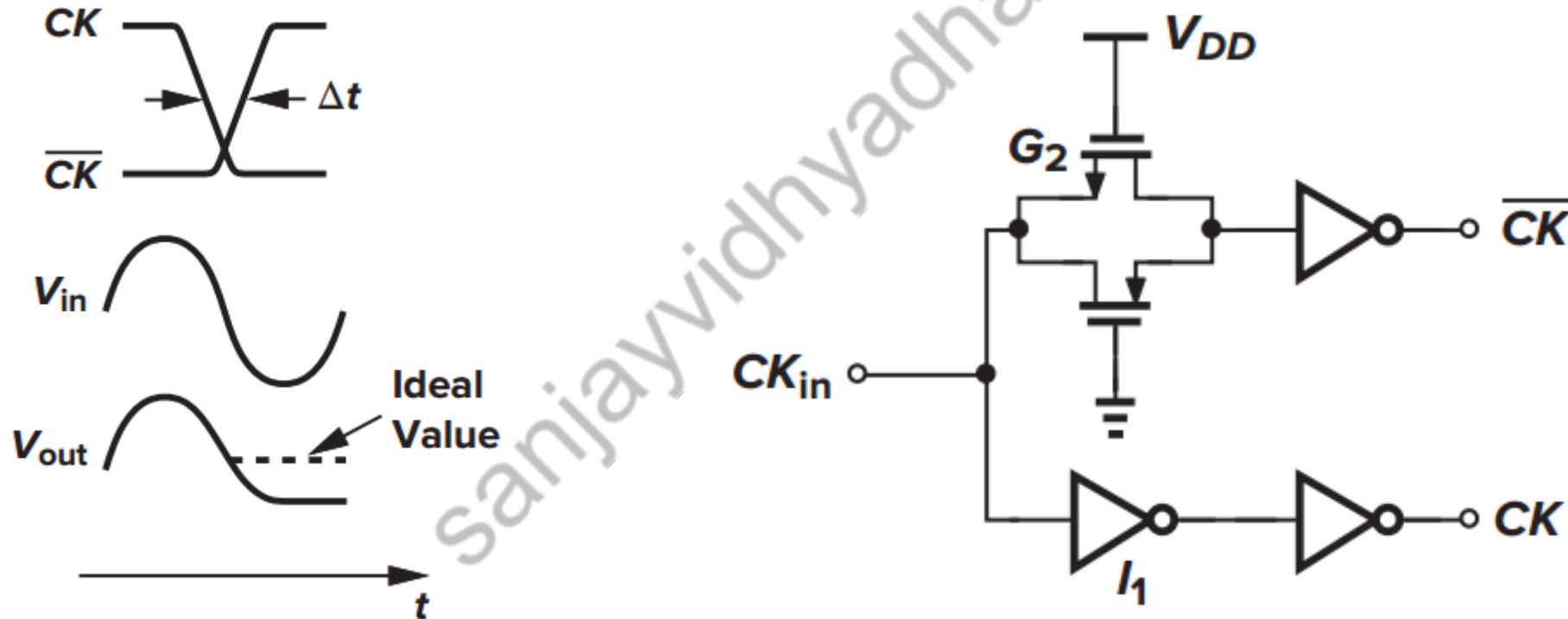
if $\mu_n C_{ox}(W/L)_N = \mu_p C_{ox}(W/L)_P$, then $R_{on,eq}$ is independent of the input level.

3. Sampling Switches

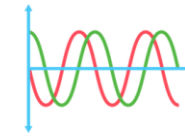


Precision Considerations

Distortion generated if complementary switches do not turn off simultaneously.

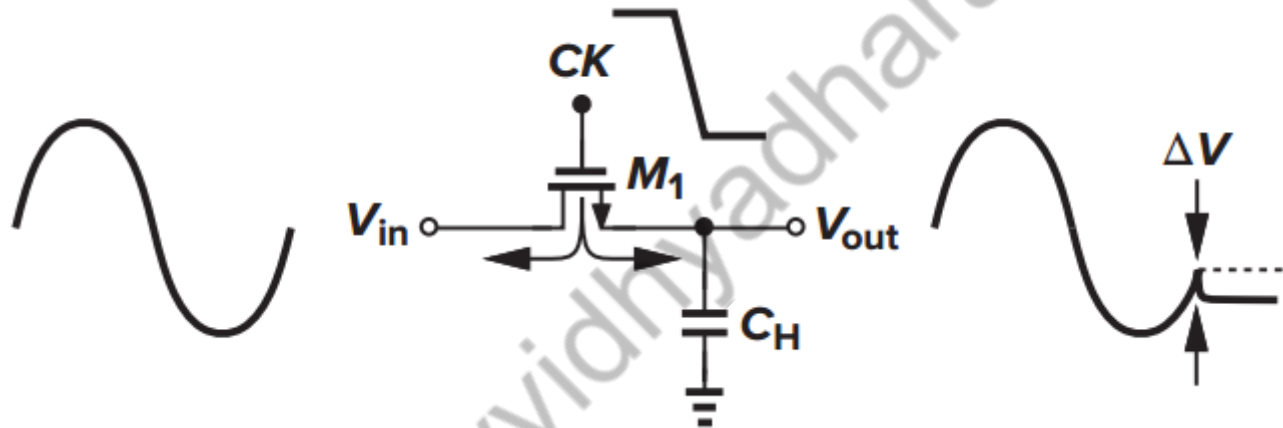


3. Sampling Switches



Precision Considerations

Charge injection



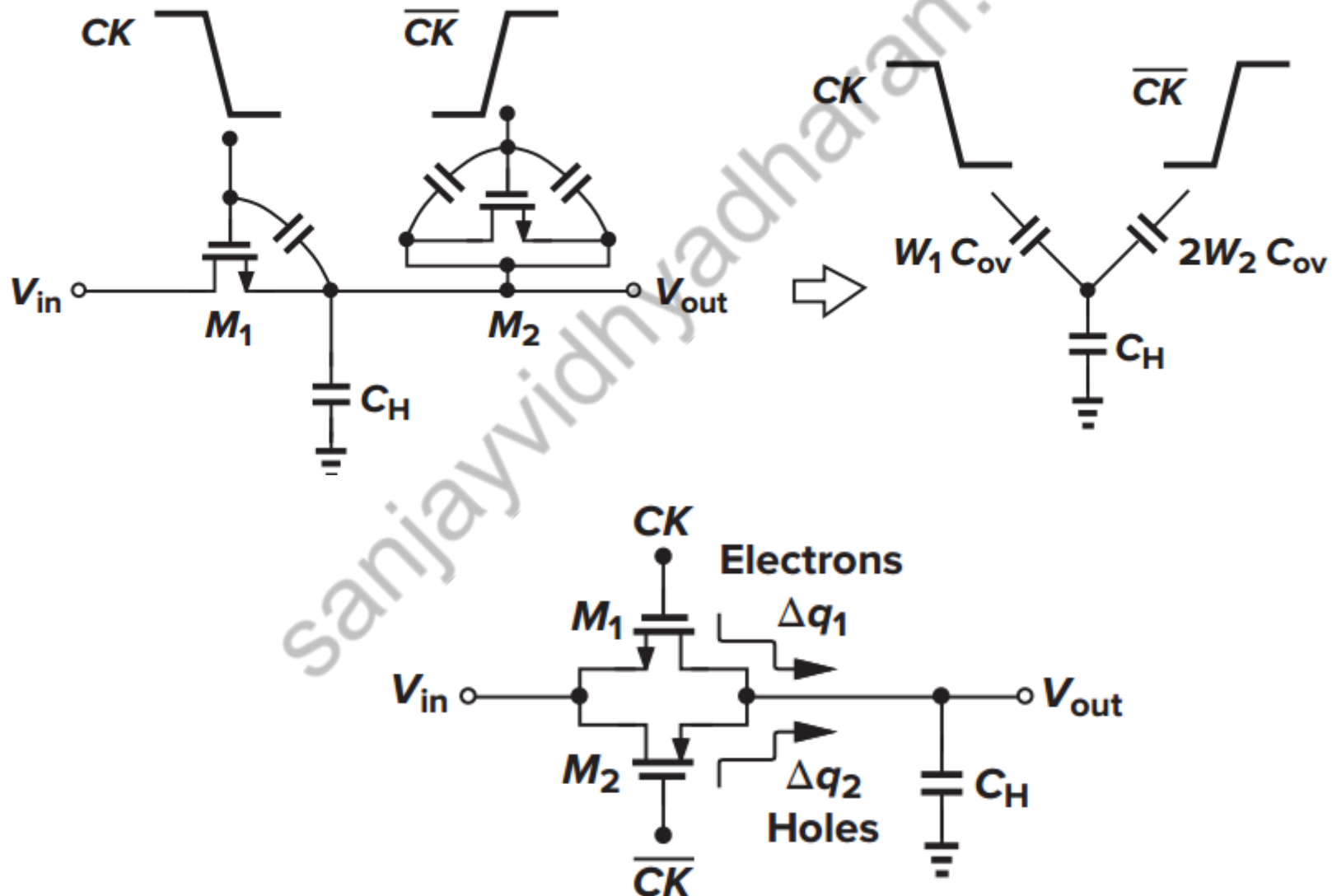
$$Q_{ch} = WLC_{ox}(V_{DD} - V_{in} - V_{TH})$$

$$\Delta V = \frac{WLC_{ox}(V_{DD} - V_{in} - V_{TH})}{2C_H}$$

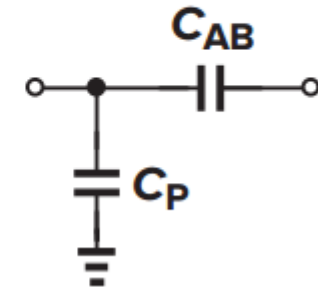
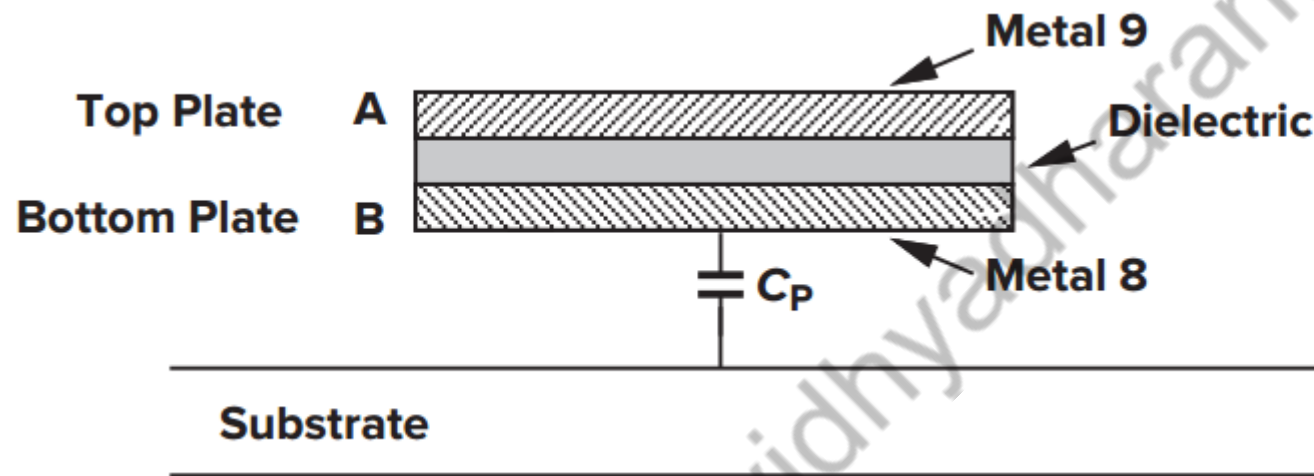
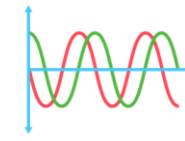
3. Sampling Switches

Precision Considerations

Clock feedthrough

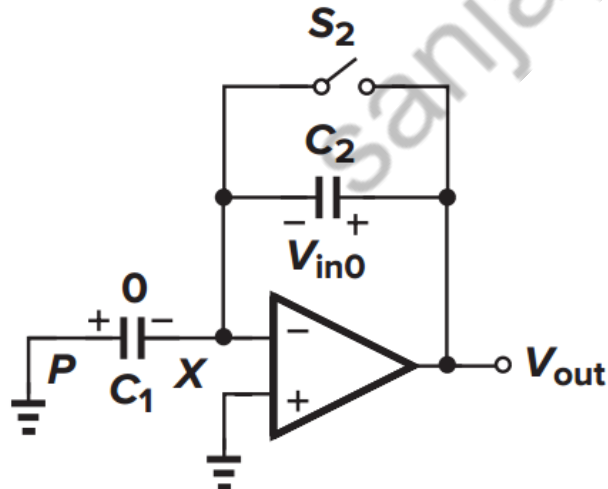
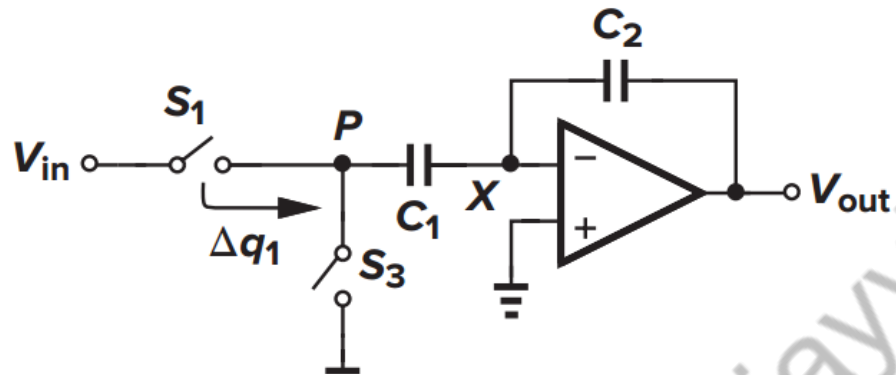
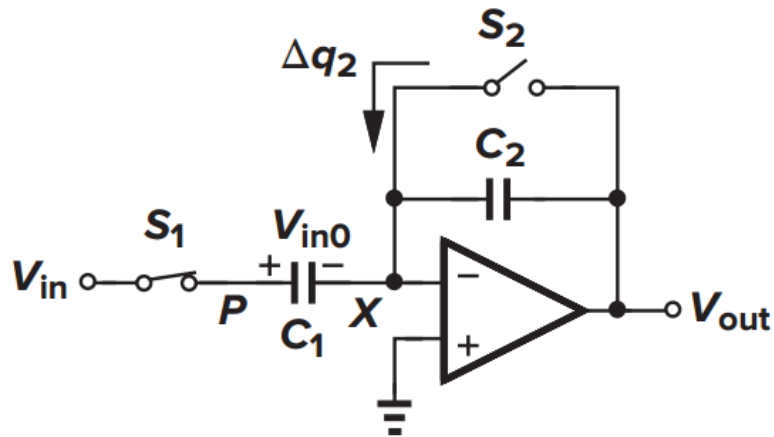
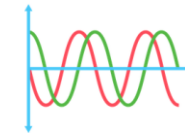


4. Implementing Capacitors

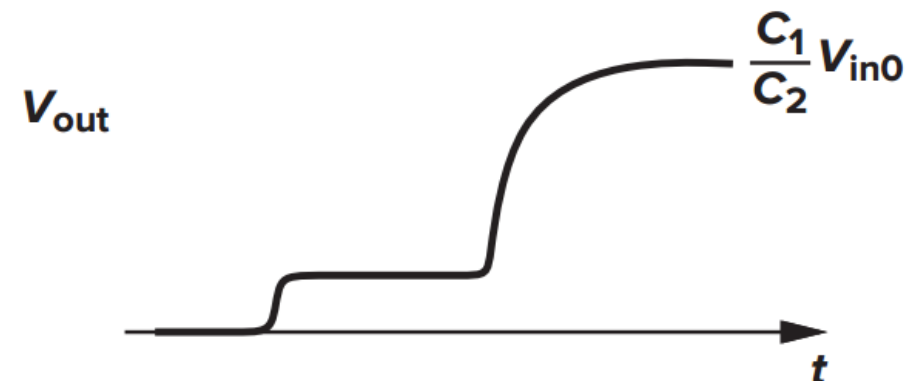
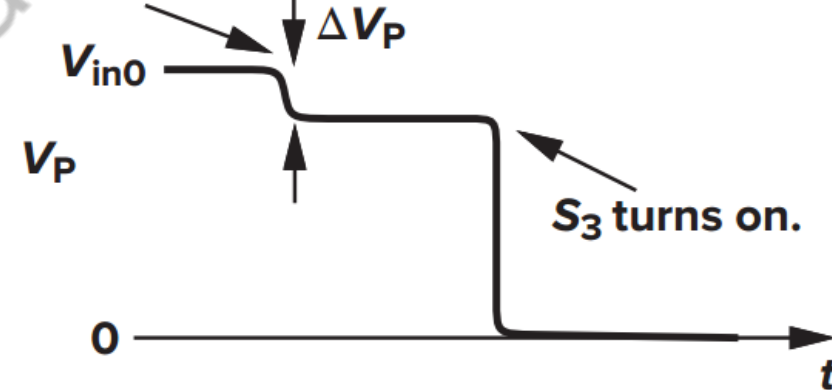


C_P , to the underlying substrate—a value typically 5 to 10% of the main capacitance

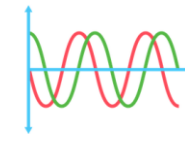
5. Switched Capacitance Amp



S_1 turns off.



6. Switched Capacitance Voltage Doubler



Precision Multiply-by-Two Circuit

Switched Capacitance Amp suffers from speed and precision degradation due to the low feedback factor

