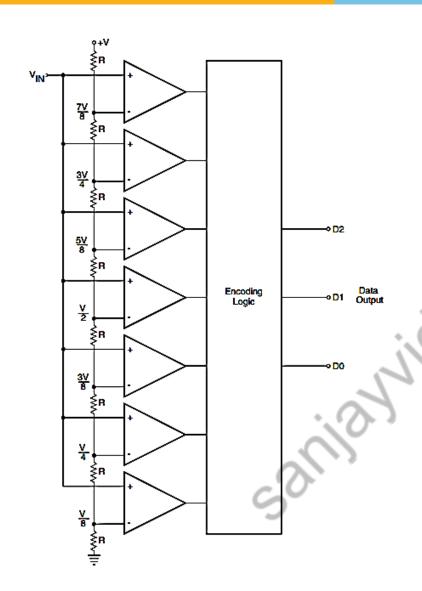


Digital Design: 2021-22

Lecture 26: ADC and DAC

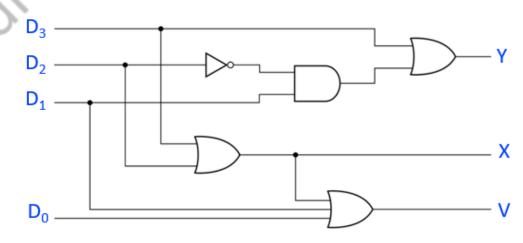
By Dr. Sanjay Vidhyadharan

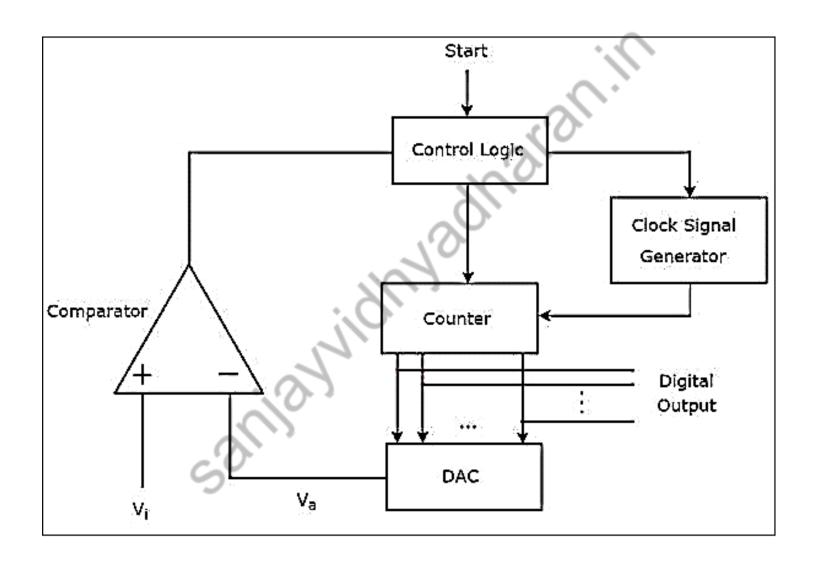
ELECTRICAL



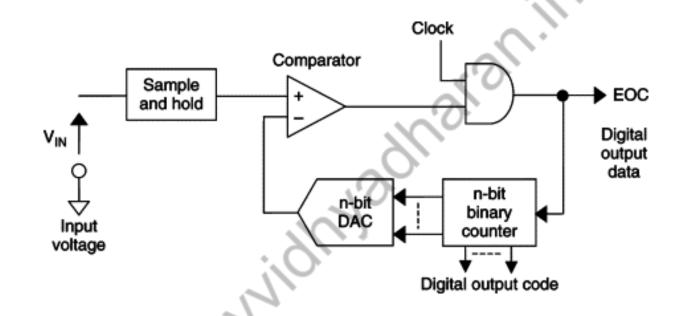
D_0	D_1	$\mathbf{D_2}$	D_3
1	0	0	0
X	1	0	0
X	X	1	0
X	X	X	1

X	Y
0	0
0	1
1	0
1	1

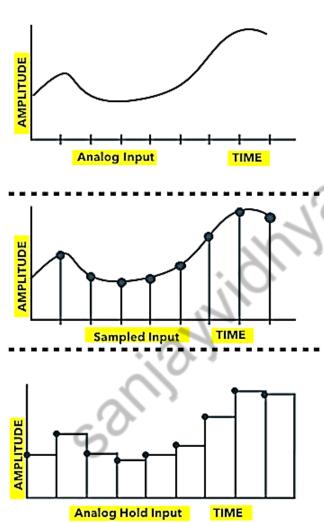




Sample and Hold

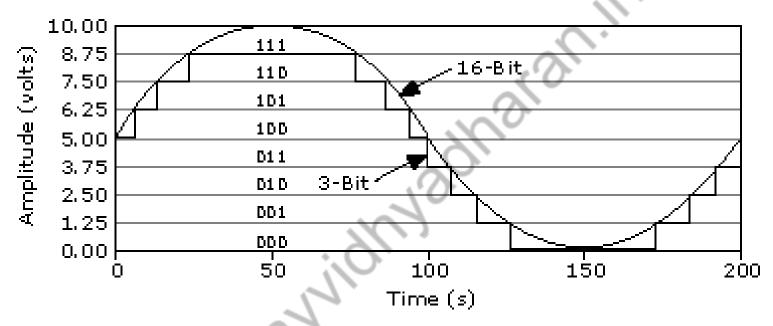


Sample and Hold



Nyquist criterion requires that the sampling frequency be at least twice the highest frequency contained in the signal, or information about the signal will be lost.

Resolution



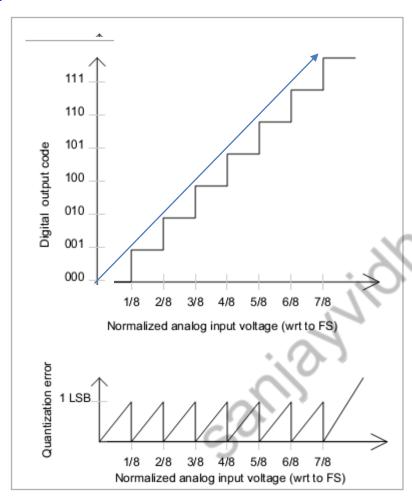
ADC Voltage Resolution =
$$\frac{(V_H - V_L)}{2^n}$$

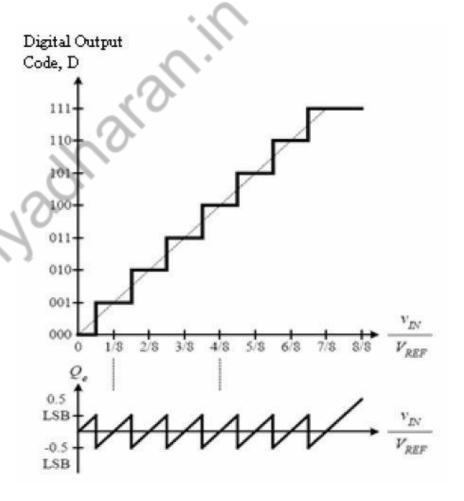
where n is the number of bits of resolution of the ADC

For
$$n = 3$$
 Resolution = $\frac{10-0}{2^3} = 1.25$

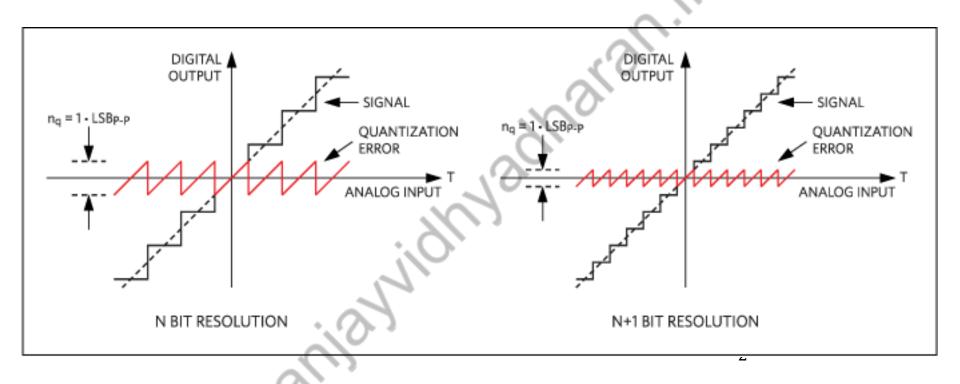
For
$$n = 16$$
 Resolution = $\frac{10-0}{2^{16}} = 0.00015$

Quantisation Error

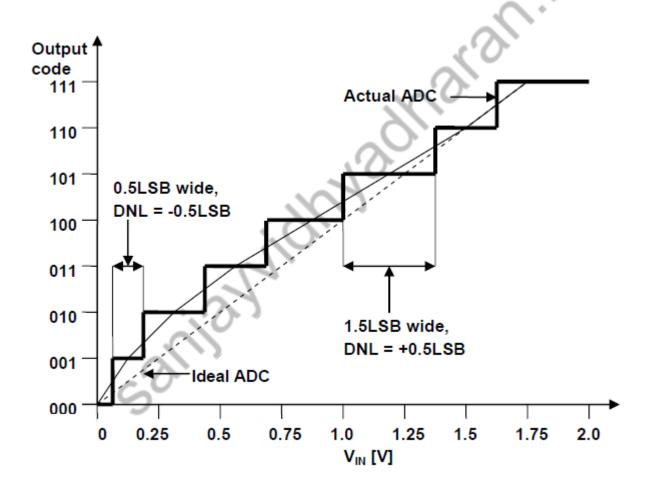




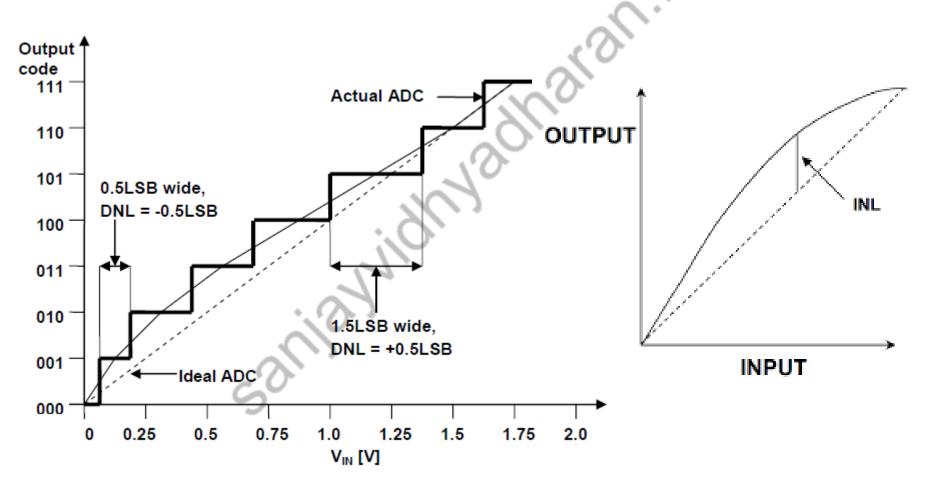
Quantisation Error



Differential Non-Linearity (DNL)



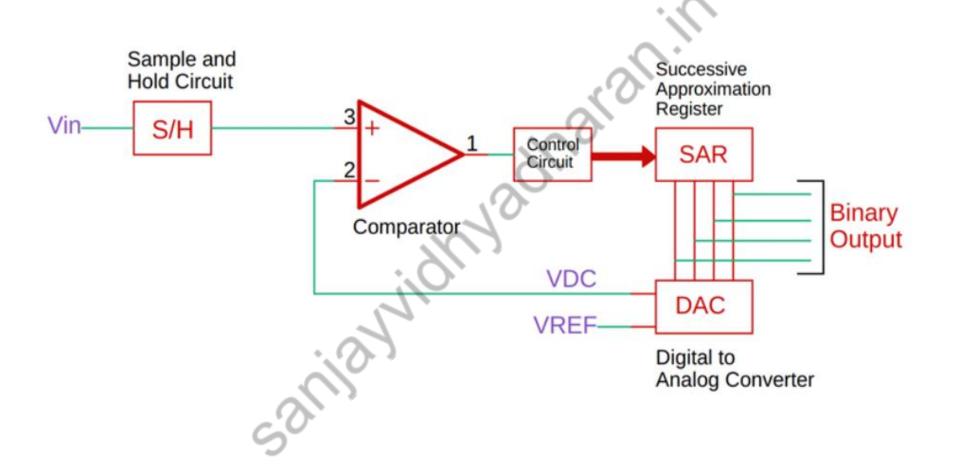
Integral Non-Linearity



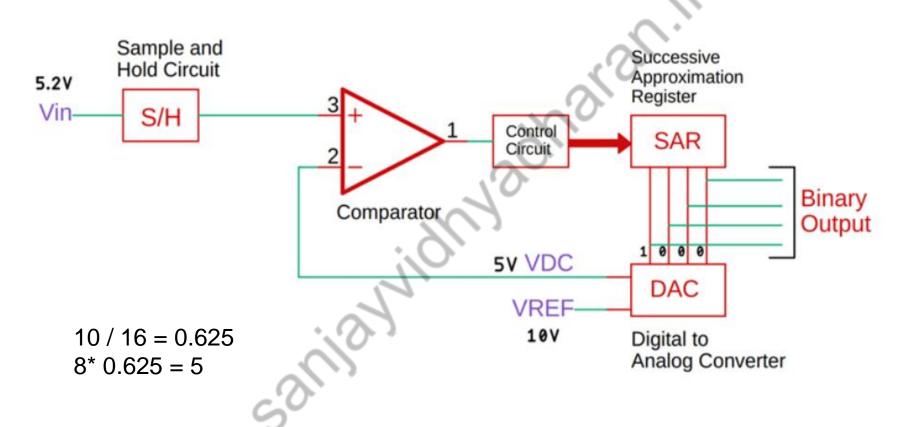
Accuracy

The accuracy specification describes the maximum sum of all errors, both from analogue sources (mainly the comparator and the ladder resistors) and from the digital sources (quantization error) of the A/D converter. These errors mainly include the gain error, the offset error and the quantization error. The accuracy describes the actual analogue input and full-scale weighted equivalent of the output code corresponding to the actual analogue input.

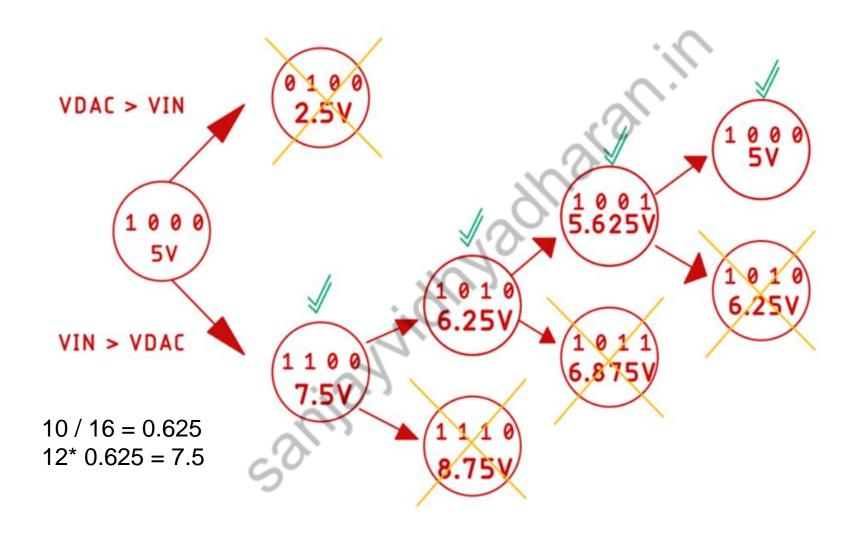
Successive Approximation ADC

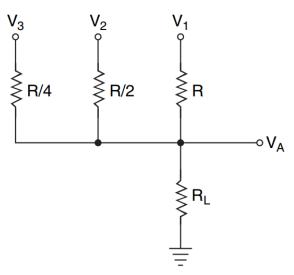


Successive Approximation ADC



Successive Approximation ADC





R_L is much larger than R

$$\frac{R}{4} || \frac{R}{2} = \frac{\frac{R}{4} * \frac{R}{2}}{\frac{R}{4} + \frac{R}{2}} = \frac{R}{6}$$

$$\frac{R}{1} || \frac{R}{4} = \frac{\frac{R}{1} * \frac{R}{4}}{\frac{R}{4} + \frac{R}{1}} = \frac{R}{5}$$

$$\frac{R}{1} || \frac{R}{2} = \frac{\frac{R}{1} * \frac{R}{2}}{\frac{R}{1} + \frac{R}{2}} = \frac{R}{3}$$

$$V_{A(V1)} = \frac{V_1 \frac{R}{6}}{\frac{R}{6} + R} = \frac{V_1}{7}$$

$$\frac{R}{1} || \frac{R}{4} = \frac{\frac{R}{1} * \frac{R}{4}}{\frac{R}{4} + \frac{R}{1}} = \frac{R}{5}$$

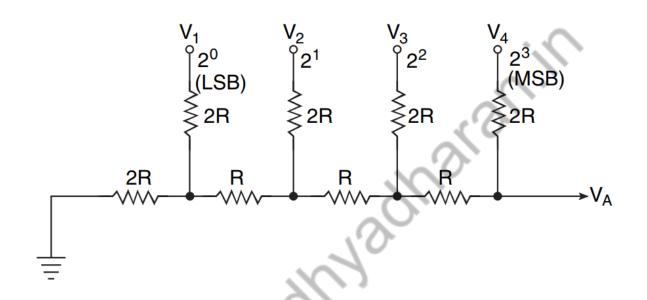
$$V_{A(V1)} = \frac{V_1 \frac{R}{6}}{\frac{R}{6} + R} = \frac{V_1}{7} \qquad V_{A(V2)} = \frac{V_2 \frac{R}{5}}{\frac{R}{5} + \frac{R}{2}} = \frac{2V_2}{7} \qquad V_{A(V3)} = \frac{V_3 \frac{R}{3}}{\frac{R}{3} + \frac{R}{4}} = \frac{4V_3}{7}$$

$$V_{A} = \frac{4V_3 + 2V_2 + V_1}{7}$$

$$V_A = \frac{4V_3 + 2V_2 + V_1}{7}$$

$$\frac{R}{1} || \frac{R}{2} = \frac{\frac{R}{1} * \frac{R}{2}}{\frac{R}{1} + \frac{R}{2}} = \frac{R}{3}$$

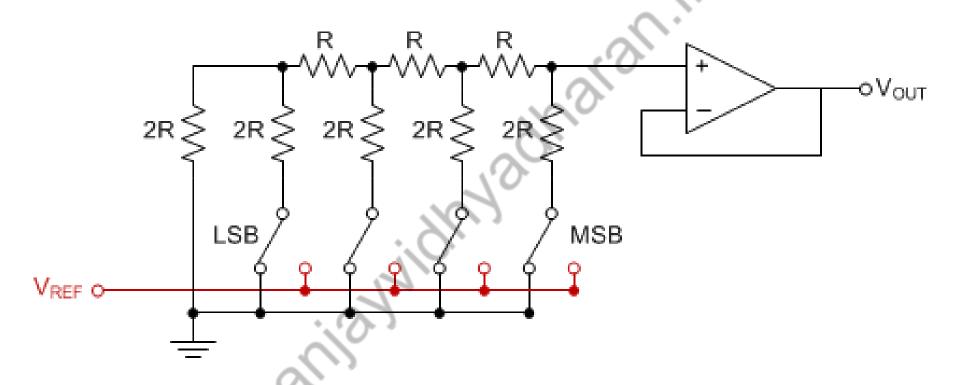
$$V_{A(V3)} = \frac{V_3 \frac{R}{3}}{\frac{R}{3} + \frac{R}{4}} = \frac{4V_3}{7}$$



$$V_{A} = \frac{V_{1} \times 2^{0} + V_{2} \times 2^{1} + V_{3} \times 2^{2} + V_{4} \times 2^{3}}{2^{4}}$$

$$V_{A} = \frac{V_{1} \times 2^{0} + V_{2} \times 2^{1} + V_{3} \times 2^{2} + \dots + V_{n} \times 2^{n-1}}{2^{n}}$$

$$V_{\rm A} = \frac{V_1 \times 2^0 + V_2 \times 2^1 + V_3 \times 2^2 + \dots + V_n \times 2^{n-1}}{2^n}$$



Resolution

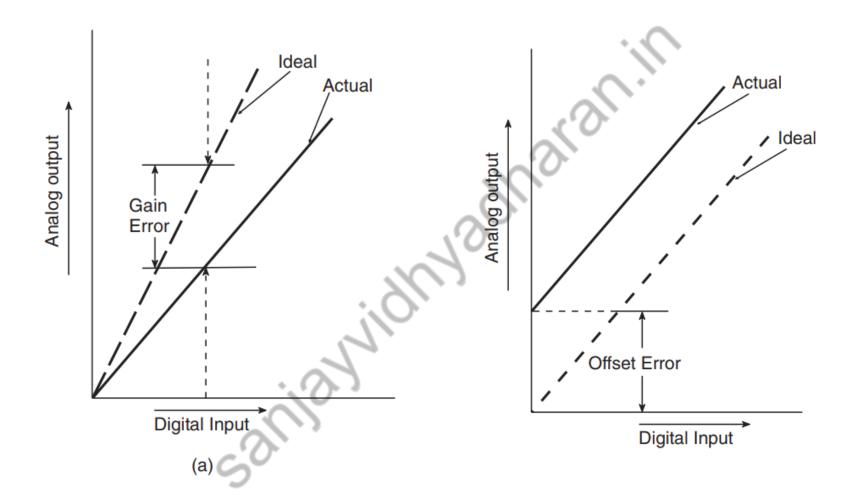
The *resolution* of a D/A converter is the number of states (2_n into which the full-scale range is divided or resolved.

An eight-bit D/A converter has 255 resolvable levels and percentage resolution of $(1/255) \times 100 = 0.39 \%$

A 12-bit D/A converter would have a percentage resolution of $(1/4095) \times 100 = 0.0244$ %.

In general, for an n-bit D/A converter, the percentage resolution is given by $(1/2_n - 1) \times 100$.

The resolution in millivolts for the two cases for a full-scale output of 5 V is approximately 20 mV (for an eight-bit converter) and 1.2 mV (for a 12-bit converter)



Accuracy

The *accuracy* of a D/A converter is the difference between the actual analogue output and the ideal expected output when a given digital input is applied.

Sources of error include the *gain error* (or full-scale error), the *offset error* (or zero-scale error), *nonlinearity errors* and a drift of all these factors.

Conversion Speed or Settling Time

The *conversion speed* of a D/A converter is expressed in terms of its settling time. The *settling time* is the time period that has elapsed for the analogue output to reach its final value within a specified error band after a digital input code change has been effected.

General-purpose D/A converters have a settling time of several microseconds, while some of the high-speed D/A converters have a settling time of a few nanoseconds. The settling time specification for D/A converter type number AD 9768 from Analog Devices USA, for instance, is 5 ns.

Thank you