



# **Digital Design**

## **First Semester 2020-21**

### **Tutorial : 13**

## **Binary Multiplication**

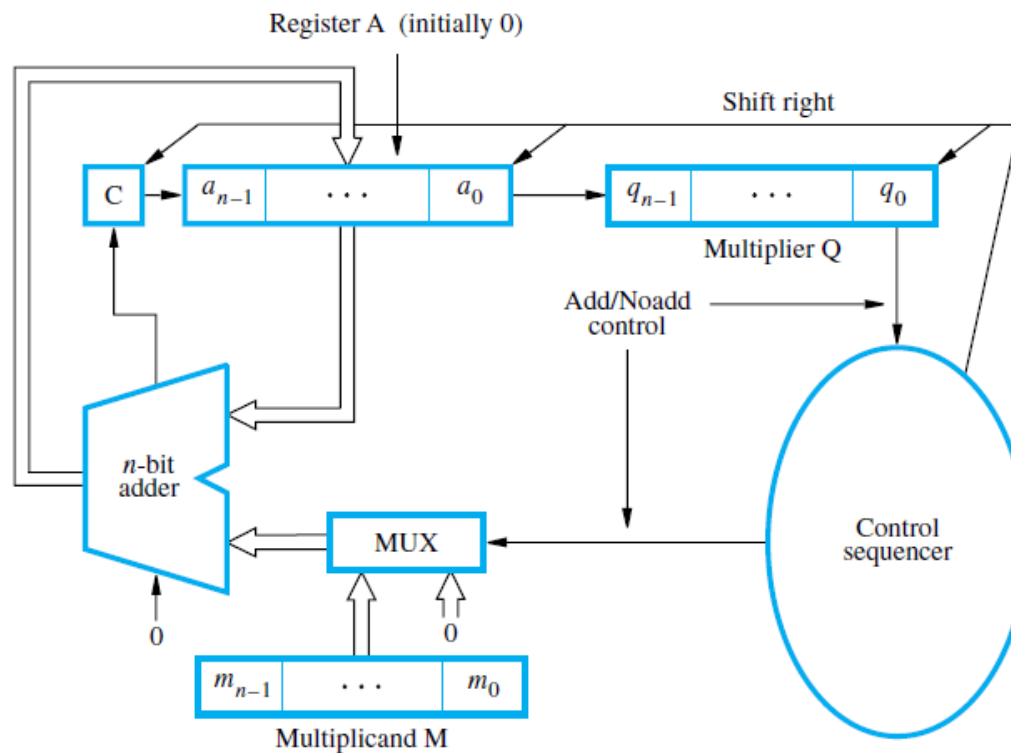
# Problem 1

1. Multiply 4 X 5 using sequential multiplier

|  |   |   |   |   |   |   |   |
|--|---|---|---|---|---|---|---|
|  |   |   |   | 1 | 0 | 0 | 0 |
|  |   |   | x | 1 | 0 | 0 | 1 |
|  |   |   |   | 1 | 0 | 0 | 0 |
|  |   |   | 0 | 0 | 0 | 0 |   |
|  |   | 0 | 0 | 0 | 0 |   |   |
|  | 1 | 0 | 0 | 0 |   |   |   |
|  |   |   |   |   |   |   |   |
|  | 1 | 0 | 0 | 1 | 0 | 0 | 0 |

# Problem 1

## 1. Multiply 4 X 5 using sequential multiplier



(a) Register configuration

# Problem 1

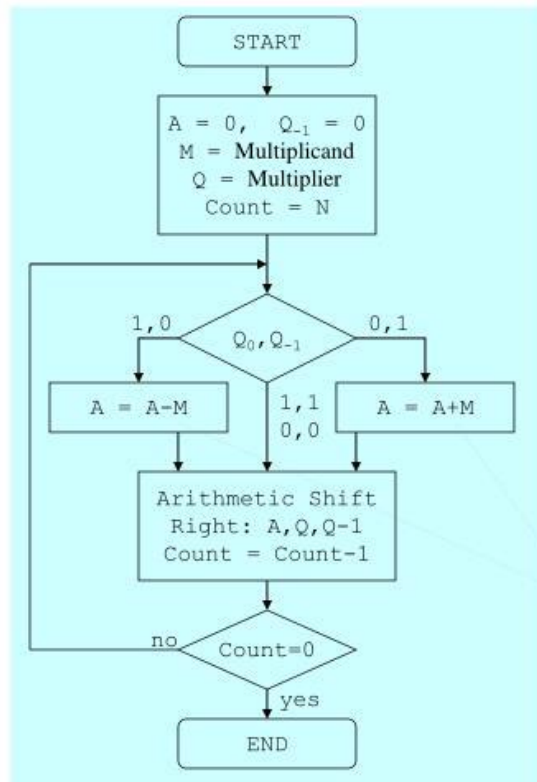
1. Multiply 4 X 5 using sequential multiplier

| 4x5 |                          |             |              |             |          |
|-----|--------------------------|-------------|--------------|-------------|----------|
|     |                          | M           | A            | Q           |          |
|     | <b>Initial Condition</b> | <b>0100</b> | <b>00000</b> | <b>0101</b> |          |
|     | <b>Load</b>              | <b>0100</b> | <b>00100</b> | <b>0101</b> | <b>1</b> |
|     | <b>Shift Right</b>       | <b>0100</b> | <b>00010</b> | <b>0010</b> |          |
|     | <b>Load</b>              | <b>0100</b> | <b>00010</b> | <b>0010</b> | <b>2</b> |
|     | <b>Shift Right</b>       | <b>0100</b> | <b>00001</b> | <b>0001</b> |          |
|     | <b>Load</b>              | <b>0100</b> | <b>00101</b> | <b>0001</b> | <b>3</b> |
|     | <b>Shift Right</b>       | <b>0100</b> | <b>00010</b> | <b>1000</b> |          |
|     | <b>Load</b>              | <b>0100</b> | <b>00010</b> | <b>1000</b> | <b>4</b> |
|     | <b>Shift Right</b>       | <b>0100</b> | <b>00001</b> | <b>0100</b> |          |

# Problem 2

## 2. Multiply -4 X 2 using Booth Algorithm

### Booth's Algorithm for 2's Complement Multiplication



M = 0101    -M = 1011  
Q = 0110  
N = 4

| A    | Q    | Q <sub>-1</sub> | N |
|------|------|-----------------|---|
| 0000 | 0110 | 0               | 4 |
| 0000 | 0011 | 0               | 3 |
| 1011 | 0011 | 0               |   |
| 1101 | 1001 | 1               | 2 |
| 1110 | 1100 | 1               | 1 |
| 0011 | 1100 | 1               |   |
| 0001 | 1110 | 0               | 0 |

Answer is in A, Q  
00011110<sub>2</sub> = 30<sub>10</sub>

Two's complement multiplication can be performed using Booth's Algorithm.

To save time, both M and -M can be computed ahead and provided as one of the inputs to the adders for A-M and A+M.

Instead of a loop, the math processor can provide separate hardware for each stage of the multiplication algorithm.

# Problem 2

## 1. Multiply -4 X 2 using Booth Algorithm

| <b>-4X2</b>              | <b>1100</b> | <b>0010</b> |            |          | <b>-M = 0100</b> |
|--------------------------|-------------|-------------|------------|----------|------------------|
|                          | <b>A</b>    | <b>Q</b>    | <b>Q-1</b> | <b>N</b> |                  |
| <b>Initial Condition</b> | <b>0000</b> | <b>0010</b> | <b>0</b>   |          |                  |
| <b>Nothing</b>           | <b>0000</b> | <b>0010</b> | <b>0</b>   | <b>1</b> |                  |
| <b>Shift Right</b>       | <b>0000</b> | <b>0001</b> | <b>0</b>   |          |                  |
| <b>Substract</b>         | <b>0100</b> | <b>0001</b> | <b>0</b>   | <b>2</b> |                  |
| <b>Shift Right</b>       | <b>0010</b> | <b>0000</b> | <b>1</b>   |          |                  |
| <b>Add</b>               | <b>1110</b> | <b>0000</b> | <b>1</b>   | <b>3</b> |                  |
| <b>Shift Right</b>       | <b>1111</b> | <b>0000</b> | <b>0</b>   |          |                  |
| <b>Nothing</b>           | <b>1111</b> | <b>0000</b> | <b>0</b>   | <b>4</b> |                  |
| <b>Shift Right</b>       | <b>1111</b> | <b>1000</b> | <b>0</b>   |          |                  |